

EQUATIONS

In what country does this scene happen ?



What is the aim of this problem ?

Let x be the weight of one bundle of cinnamon sticks. x is the **unknown**, it's the value you have to find.

Write the equation corresponding to the situation :

Solve it.

Method for solving a linear equation of the form $ax+b=cx+d$

Transpose like-terms : $ax+b-b-cx=cx+d-b-cx$

Compute : $ax-cx=d-b$

Thus $(a-c)x = d-b$

Thus $x = \frac{d-b}{a-c}$

The solution of the equation is $\frac{d-b}{a-c}$.

Task 1 Solve the following equations

$$4u + 5 = 5u - 30$$

$$3r + 10 = 2r + 20$$

Task 2

Sales at the fishmonger's !

« Look at my fishes, they are so good ! A slice of tuna is worth two soles !...Four soles and two slices of tuna are 28 £ ! »

Determine the price of one sole.



Equations

Task 3

The aim of the exercise is to conjecture the solution of a problem using a mathematics software named « GEOGEBRA ». The situation of the problem is given below :

$ABCD$ is a **rectangle** such that $AB=7$ and $AD=4$. M is a point moving on the segment $[CD]$.

1. Open Geogebra. Switch it to English.
2. Build $ABCD$ and M . Build the **trapezium** $ABMD$ and the triangle BCM . Build the segment $[DM]$.
3. Their areas are displayed in the Algebra Window ($poly1$ and $poly2$). Let's call A the double of $poly2$. Write it in the Input Field and display it in the Algebra Window.
4. Move the point M and find approximately the position for which the area of the trapezium is **twice** the area of the triangle.

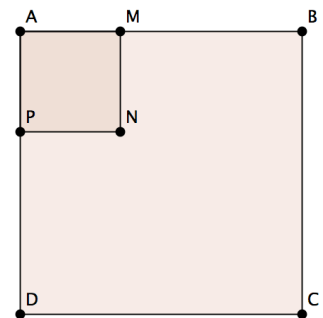
Conjecture : When $DM \approx \dots\dots\dots$, we have $A = poly1$. The area of the trapezium is twice the area of the triangle.

Proof : Let x be the length of the segment $[DM]$.

1. Find the expression of the area of $ABMD$ in terms of x .
2. Find the expression of the area of BCM in terms of x .
3. Write the equation corresponding to the problem and solve it. Check the previous conjecture.

Task 4 : Four skirts and five ties cost 340£. Given the price of a shirt is three times the price of a tie, find the price of each.

Task 5 : $ABCD$ is a square of side 20. Let M be a point of $[AB]$. We **denote** $x=AM$. P and N are such that $P \in [AD]$ and $AMNP$ is a square.



Let $f(x)$ be the area of $AMNP$ and $g(x)$ be the area of the triangle DNC .

1. Express $f(x)$ and $g(x)$ in terms of x .
2. Find x such that $f(x) = g(x)$.

Task 6 Let $A(x) = 2(x + 3)^2 + 6 + 2x$.

1. Factor $A(x)$.
2. Expand $A(x)$.
3. Compute $A(0)$, $A(1)$, $A(\sqrt{7})$.
4. Solve the equation $A(x)=0$.
5. Solve the inequation $A(x)>24$.

Task 7 Let $A(x) = (x - 1)^2 - (3x - 6)^2$.

1. Expand $A(x)$.
2. Factor $A(x)$.
3. Compute $A(0)$, $A(\frac{7}{4})$, $A(1 - \sqrt{2})$.
4. Solve the equation $A(x) = 0$.
5. Solve the inequation $A(x) > 0$.

SPECIAL PRODUCTS

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

$$(a - b)(a + b) = a^2 - b^2$$